Atomization of correlated molecular-hydrogen chain: A fully microscopic Variational Monte-Carlo solution

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Outline



- 2 Methods
 - EDABI + VMC Model Hamiltonian
- 3 2H Chain State function Structure
- Electronic properties Metallicity Correlation functions
- 6 Conclusions

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R. P. Dias, I. F. Silvera, Science 10.1126/science.aal1579 (2017)



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Metalization of Hydrogen

Metalic state

- E. Wigner i H. B. Huntington,
- J. Chem. Phys. 3, 764 (1935):
 - H H distance (d_{HH}) ,
 - Wigner-Seitz radius $(r_s \equiv (\frac{3}{4\pi n})^{1/3})$

Metalization at $p \approx 25 \, GPa$: $2 r_s > d_{HH}$.



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Superconductor

- N. Ashcroft, PRL **21**, 1748 (1968) $T_C = \Theta_D \mathcal{F}(\lambda(r_s))$
 - ⊖_D Debye Temperature,
 - λ electron-phonon coupling.

	rs (a0)	<i>Тс</i> (К)
Jupiter surface	0.1	2e – 27
Jupiter core	0.8	283.4



en.wikipedia.org/wiki/Metallic_hydrogen Jupiter core: superconductor with $T_C \sim 300~K$?

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Exact Diagonalization Ab Initio (EDABI) + VMC



Sources

♠ J. Spałek et al., Phys. Rev. B 61, 15676 (2000);
 ♠ APK et al., Eur. Phys. J. B 86, 252 (2013);
 ♦ A. Biborski, APK, J. Spałek, Comput. Phys. Commun. 197, 7 (2015);
 ♥ A. Biborski, APK, J. Spałek, Phys. Rev. B 98, 085112 (2018).

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Methods

Model

For details see: Phys. Rev. B **98**, 085112 (2018)



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Assumptions

(a) two hydorgen atoms in the unit cell (α, β), with the lattice parameter a and bond length b;
(b) range of the hoppings terms extends up to 2a;
(c) interactions counted up to the range of 2a.

"Infinite" crystal

♂ Periodic Boundary

Conditions;

- 🔿 supercell of 17, 21, 25,
- 33 and 37 unit cells;

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Methods

Hamiltonian

Hamiltonian

Second quantization

$$\begin{split} \mathcal{H} &= \sum_{i} \epsilon_{i} (\hat{n}_{i\uparrow} + \hat{n}_{i\downarrow}) + \sum_{i \neq j} t_{ij} (\hat{c}_{i\uparrow}^{\dagger} \hat{c}_{j\uparrow} + \hat{c}_{i\downarrow}^{\dagger} \hat{c}_{j\downarrow}) \qquad // \text{ free electrons} \\ &+ \sum_{i} U_{i} \hat{n}_{i\uparrow} \hat{n}_{i\downarrow} + \sum_{i \neq j} K_{ij} \hat{n}_{i} \hat{n}_{j} \qquad // \text{ interactions} \end{split}$$

First-to-second-quantization calculation step

$$t_{ij} \equiv \left\langle w_i(\mathbf{r}) \middle| - \nabla^2 - \sum_{l \in \text{ions}} \frac{2Z}{|\mathbf{R}_l - \mathbf{r}|} \middle| w_j(\mathbf{r}) \right\rangle \qquad \epsilon_i \equiv t_{ii}$$

$$V_{ijkl} \equiv \left\langle w_i(\mathbf{r}) w_j(\mathbf{r}') \middle| \frac{2}{|\mathbf{r} - \mathbf{r}'|} \middle| w_k(\mathbf{r}) w_l(\mathbf{r}') \right\rangle \qquad U_i \equiv V_{iiii}, \ K_{ij} \equiv V_{ijij}$$

Dimensionality - 1D chain in 3D space

- w_i(r) build from 1s Slater orbitals;
- Coulomb potential $V_C(\mathbf{R}) \propto |\mathbf{R}|^{-1}$;

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Proper state function

One-dimensional enthalpy

$$h \equiv f \frac{a}{2} + \frac{E}{N},$$

with f as an external force (analogue of the pressure), the lattice parameter a, and ground-state energy Efor the N-particle supercell.

Run for given fImage: Opt. structureImage: Opt. wavefunctionImage: Opt. Jastrow

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Structure

Results for finite systems



Peierls-like distortion from First Principles for a correlated system

- No distortion for small systems.
- Molecular → atomic transition at high "pressure"

 \hookrightarrow see my poster after lunch.

for finite systems cf. also E. Giner et al., J. Chem. Phys. 138, 074315 (2013).

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Structure

Thermodynamic limit



Conditions of molecular-to-atomic transition for $N \to \infty$

- finite-size scaling of atomization lattice parameter $a_{dim} \approx 1.17 a_0 > 0;$
- finite-size scaling of atomization force $f_c \approx 6.02 \frac{Ry}{30} < \infty$.

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Metallicity of hydrogen chain

Point of reference

We use the parameters of the Hamiltonian for N = 50 for the reference.

Charge gap

 $\Delta_N \equiv \left. \frac{E_{N+4}-2E_N+E_{N-4}}{4} \right|_{@h(f)} \\ E_N \text{ - the ground state of the } \\ N\text{-particle system described} \\ \text{by the reference Hamiltonian} \\ \text{with the structure minimizing} \\ \text{effective enthalpy.} \end{cases}$

Thermodynamic limit

$$\Delta \equiv \Delta_{\infty} = \lim_{N \to \infty} \Delta_N$$



Example of finite-size scaling for charge gap Δ .

Closing of the charge gap



Apparent metallicity of the hydrogen chain in the atomic phase

- charge gap closed at the MLC \rightarrow ALC transition;
- further-than-nearest neighbor hoppings;
- chain exist in 3D (both single-particle wavefunctions and Coulomb potential are taken for D = 3);

in agreement with L. Stella et al., Phys. Rev. B 84, 245117 (2011)

Density-density correlation

Density-density correlation



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Spin-spin correlation

Spin-spin correlation



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Conclusions

Conclusions

Hydrogen chain

- Peierls-like distortion at ambient "pressure";
- correlations do not weaken distortion;
- external force induces molecular \rightarrow atomic transition;
- concomitant atomization and metallization ;
- no long-range order;



Dziękuję za uwagę

Thank you for your attention

